



# Classifying Capabilities

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Capture checking in Scala 3 enables lightweight and practical effect and resource tracking by recording capabilities in types. However, the system offers no way to reason about *kinds* of capabilities. Natural constraints such as “retaining only the control-flow capabilities of this closure” or “excluding all thread-local capabilities from this argument” become inexpressible. Both arise in the Scala 3 standard library: Try re-throws caught exceptions, so it retains only the control-flow capabilities of its body, and Future must not capture thread-local resources. The inability to state these constraints has kept parts of the library outside capture checking.

We introduce *capability classifiers*: a tree-structured, user-extensible hierarchy of tags that classify capabilities by their semantic role. *Projections* filter capture sets by classifier, supporting both inclusion (c. **only**[C]) and exclusion (c. **except**[C]). The tree structure enables decidable disjointness reasoning: classifiers on separate branches are guaranteed to be disjoint regardless of unknown extensions elsewhere in the hierarchy. We formalize classifiers as an extension of System Capless, a core calculus for capture checking, introducing a classifier kind algebra based on intersection, union, and subtraction of classifier subtrees. We extend the operational semantics to model exception interception and establish type safety, effect safety, and handler coverage via a big-step proof, fully mechanized in Lean 4. Classifiers are implemented in the Scala 3 capture checker, and we demonstrate their use on standard library types and real-world effect exclusion patterns.

CCS Concepts: • **Software and its engineering** → **Constraints**; *Control structures*.

Additional Key Words and Phrases: Scala, Capture Checking, Effect Exclusion, Exception Handling

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## 1 Introduction

Capture checking [5] provides a lightweight discipline for tracking effects as capabilities. A *capability* is a value whose possession grants the authority to perform an effect or access a resource, such as a file handle, a network socket, a mutable reference, or a token that permits throwing exceptions. By recording which capabilities a term may use in its *capture set*, the type system enforces lexically scoped bounds on side effects: a function’s type signature declares which capabilities it may use, and the compiler statically checks that these bounds are respected. It has been integrated into Scala 3, and has been applied to large parts of the standard library, including the collections [60].

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Two notable parts of the standard library have raised difficulties when adopting capture checking: exception handling via `Try[T]` and asynchronous computation via `Future[T]`. The difficulty lies not in tracking *individual* capabilities, but in reasoning about *kinds* of capabilities.

Consider `Try[T]` [43]: its constructor executes a closure and catches any thrown exceptions, packaging the result as a success-or-failure value.

```
val result: Try[String] = Try(file.read())
val content: String = result.get // may re-throw IOException
```

The constructor takes its argument by-name, so `file.read()` is not evaluated at the call site. Instead, it is implicitly wrapped in a closure that the constructor runs internally. In this example, `Try` catches exceptions thrown by `file.read()` and wraps them as a value. The resulting `Try` is pure with respect to most capabilities, since e.g., the file handle is not retained. However, it is *not* pure with respect to control-flow capabilities such as `CanThrow` [32] labels: calling `.get` may re-throw the caught exception, which exercises that capability. Without a way to express “the control-flow subset of the closure’s captures,” the type of `Try`’s constructor must be either too permissive (unsoundly claiming purity) or too conservative (retaining all captures).

A dual problem arises with `Future[T]`. Its constructor dispatches a closure to a thread pool, where it may execute on an arbitrary carrier thread.

```
boundary: label =>
  Future:           // should reject: label is thread-local
    break(0, label) // non-local return to another thread's stack
    file.read()
```

As with `Try`, the `Future` constructor takes its body by name, and Scala’s colon syntax passes the indented block as that argument. Here, `boundary` introduces a `Label` capability that is tied to the originating thread’s stack. Using it inside the `Future` closure would attempt a non-local return across threads, which must be rejected. More generally, capabilities such as thread-local storage, stack-based control flow, and native interop must not leak into the closure. Yet existing capture checking provides no mechanism to *exclude* an entire category of capabilities from a capture set. One can only enumerate specific capabilities as an upper bound.

Both problems share a common root: capture sets track capabilities by identity, but lack the vocabulary to classify capabilities by *kind*. There is no way to filter a capture set to retain only capabilities of a certain kind, nor to exclude all capabilities belonging to another. These are precisely the operations needed to give accurate constraints to `Try` and `Future`, and, as we demonstrate, to many patterns beyond the standard library. The missing abstraction is not better tracking of individual capabilities, but operators that project and exclude whole categories of capabilities.

We propose *capability classifiers*: a tree-structured, user-extensible system of tags that classify capabilities by their semantic role. Each capability is associated with a classifier drawn from a tree-structured universe. Capture sets are enhanced with *projections* that filter by classifier *kinds*, which consist of classifier subtree inclusions (c.`only`[C]) and exclusions (c.`except`[C]). With classifiers, the previously problematic signatures become precise:

```
object Try:
  def apply[T](body: () => T): Try[T]^{body.only[Control]}
object Future:
  def apply[T](body: () -> {any.except[ThreadLocal]} T): Future[T]^{body}
```

That is, `Try` retains only control capabilities from its argument, while `Future` requires its argument to exclude thread-local ones.

The tree structure of classifiers is chosen to fit the setting that Scala-like languages inhabit: an open ecosystem of separately compiled modules. The tree is open, since any classifier can be extended with sub-classifiers in a separate module, yet disjointness remains decidable and stable under such extensions: classifiers on different branches stay disjoint even as sub-classifiers are later added by other modules. Hierarchical classification, filtering, and exclusion each have precedents in effect systems, for instance as boolean algebras [24, 9] or lattices of qualifiers [18]. Our contribution is their integration with capture checking, where the filtered sets contain references to program values rather than abstract effect labels, under the modularity constraints that separate compilation imposes on a language like Scala. We explain this design point in Section 6.1.

Beyond the standard library, we show that classifiers enable many practical patterns: restricting parallel computations to read-only capabilities, modeling privilege qualifiers on transaction objects, and encoding the effect exclusion patterns catalogued by Lutze et al. [24] in real-world codebases. The result is a lightweight extension to capture checking that makes previously awkward library interfaces precise without abandoning the existing capability-based account.

To summarize, our contributions are as follows.

- We introduce capability classifiers for Scala 3 capture checking, motivated by standard-library examples and real-world effect exclusion patterns that require reasoning about capabilities by kind rather than by identity (Section 2).
- We design a tree-structured, user-extensible classifier hierarchy with a decidable kind algebra supporting union, intersection, subtraction, and disjointness, chosen to preserve modular extension under separate compilation (Section 3.1).
- We formalize capture checking with capability classifiers as System Capless( $\mathcal{K}$ ), an extension of System Capless [60] with kind-annotated projections and capture kinding, and prove type safety with a checked big-step semantics, fully mechanized in Lean 4. In contrast to prior capture-checking metatheories based on syntactic progress and preservation, the big-step account lets us reason directly about closure properties of evaluation, yielding not only type and effect safety, but also used label prediction, capture prediction and handler coverage (Sections 3 and 4).
- We implement classifiers in the Scala 3 capture checker, demonstrate them on standard-library types and on real-world effect exclusion patterns, discuss the resulting design decisions, and report on the impact of classifiers in the capture-checked standard library (Sections 5 and 6).

Finally, we review related work in Section 7 and conclude in Section 8.

## 2 The Case for Classifiers: Capability Kinds in Scala

Capture checking [5, 60, 44] extends Scala’s type system to track *capabilities*, informally values “of interest”, such as file handles, access-permission tokens, or mutable data structures. In capture checking, types also record which capabilities are used or held, or *captured*, by values of that type. These *capturing types* have the form  $\tau^{\{x_1, \dots, x_n\}}$ , which includes the shape type  $\tau$  and the *capture set*  $\{x_1, \dots, x_n\}$ . Capture sets give an upper bound on capabilities that can be accessed by values of the type. A pure type, written  $\tau^{\{\}}$  or just  $\tau$ , cannot capture any capabilities.

By making capability dependencies visible in types, capture checking serves as a lightweight effect system: the capabilities a function closes over precisely describe the effects it may perform, enabling fine-grained control over what each piece of code is allowed to do.

The conventional function type  $A \Rightarrow B$  is shorthand for  $(A \rightarrow B)^{\{\text{any}\}}^1$ , a function that may capture arbitrary capabilities. In contrast, the pure function type  $A \rightarrow B$  carries an empty capture set and therefore cannot close over any capability. For example, in the following code, `run` declares that its callback task may only use the `net` capability:

<sup>1</sup>The universal capability `any` was referred to as `cap` in older works.

```

trait ThreadLocal extends Classifier, SharedCapability
trait Control      extends Classifier, ThreadLocal

class CanThrow[-T] extends Control

case class Environment(file: File, exc: CanThrow[Int])

def runOnNewThread(task: () ->{any.except[Control]} Unit)

def f(env: Environment) =
  // ok: env.file is not Control
  runOnNewThread(() => env.file.read())

  // error: exc is Control
  runOnNewThread:
    given CanThrow[Int] = env.exc
    throw 1

```

Fig. 1. Classifiers in Scala: declarations (left) and excluding the Control category with `.except` (right).

```

def main(fs: Filesystem^, net: Network^): Unit =
  def run(task : () ->{net} Unit) = task()
  run(() => net.send(fs.read("secret"))) // error: fs not in {net}

```

Here `task` has type `() ->{net} Unit`, a shorthand for `() -> Unit{net}`. The capture set `{net}` makes explicit that this function may only use the `Network` capability held by `net`. Any attempt to capture `fs`, which has type `Filesystem*` (i.e., `Filesystem*{any}`), is rejected because `fs` is not in the capture set.

Capabilities are extremely versatile: they can express concepts from many different domains, such as exceptions, I/O, mutation, and more. However, capture sets may only mention capability *identities*. This means it is not possible to:

- (1) limit entire *kinds* of capabilities based on system specifications or user definitions (e.g., all control-flow-related capabilities);
- (2) refer to a *subset* of capabilities captured by a given reference, filtered by such kinds (e.g., only the read-only subset of a mutable data structure); or
- (3) exclude capabilities from a capture set.

At the heart of this problem lies the lack of a classification mechanism for capabilities and the inability to include or exclude them based on that classification. We introduce *classifiers*, a hierarchical system and algebra for classifying capabilities. In this section, we give an informal introduction to classifiers in Scala and showcase the need for them in the standard library.

## 2.1 Capability Classifiers

A *classifier* is a tag drawn from a tree-structured hierarchy that describes the semantic role of a capability. Each classifier has exactly one parent but may have arbitrarily many children. Because every path from a classifier to the root is unique, a capability can be assigned to exactly one classifier while still being recognized as belonging to every ancestor of that classifier. The root of the tree is the built-in classifier `Capability`, provided by the standard library. The standard library also provides two children of `Capability`: `SharedCapability`, for capabilities safe to share across scopes, and `ExclusiveCapability`, for exclusively owned resources.

**Defining classifiers.** In Scala, classifiers are represented as traits. A new classifier is introduced by defining a trait that extends the marker trait `Classifier` and a parent classifier (Figure 1, top left). This declares `Control` as a child of `ThreadLocal`. Because classifiers form an open tree, new children can be added to any classifier in a separate module without modifying existing definitions.

**Classifying capabilities.** A Scala class is associated with a classifier by extending the classifier trait *without* the `Classifier` marker (Figure 1, left). `CanThrow` is a capability [45] that tracks possibly-thrown exceptions of type `T`. Every instance of it is thereby tagged with the `Control` classifier, which lets the type system distinguish it from unrelated capabilities such as file handles. The `-T` syntax declares that `CanThrow` is contravariant: the more precise `T` becomes, the smaller the set of values that can be thrown.

```

object Try: /* before classifiers */
  def apply[T](body: () => T): Try[T]

class Try[+T]:
  def get(): T = /* re-throw if needed */

object Try:
  /* with classifiers */
  def apply[T](body: () => T): Try[T]^(body.only[Control])

```

Fig. 2. Try[T] signatures before classifiers (left) and with classifiers (right).

**Projections: .only and .except.** Given a capture reference *a*, *a*.only[*C*] denotes the subset of capabilities reachable through *a* whose classifier is *C* or any descendant of *C*. Dually, *a*.except[*C*] denotes the subset whose classifier is *not* *C* or any descendant of *C*. These two *projections* also apply to the root capability *any* to constrain an arbitrary capture set by classifier. Projections can be chained: *any*.only[SharedCapability].except[Control] restricts to shared capabilities outside Control.

With these tools in hand, consider the example of Figure 1 (right). An environment bundles a file handle and an exception-throwing capability. A function that dispatches work to a new thread must forbid its closure from using thread-local capabilities, such as exception throwing, and the .except projection expresses this constraint directly. The capture set {*any*.except[Control]} is polymorphic: it accepts any capability *except* those under Control. Accessing the File is allowed because files are not Control, while throwing exceptions using the CanThrow capability [32] is rejected at compile time.

## 2.2 Case Study: Try[T] Captures Control Capabilities

Try[T] [43] is a sum type representing either a successful value or an arbitrary runtime exception, enabling fluid conversion between exception-based and monadic error handling. Under previous capture checking, the constructor and re-throwing accessor had the signatures in Figure 2 (left). The constructor Try.apply takes a computation with arbitrary captures, yet the resulting Try[T] is declared *pure*. At first glance this seems correct: Try.apply evaluates body, catches any exception, and stores the outcome; it does not retain a reference to the closure itself.

However, this signature overlooks a particular class of capabilities that govern exception throwing. CanThrow capabilities [32, 45] track possibly-thrown exceptions through types, and boundary/break’s Label capability [46] tracks the ability to perform non-local returns. Both are classified under Control. When Try.get re-throws a stored exception, it is effectively *using* the Control capabilities that were in scope when the exception was originally thrown. Therefore Try[T] is not truly pure: it retains the Control capabilities of the closure. With classifiers, this dependency can be stated precisely (Figure 2, right). The projection body.only[Control] selects only the subset of body’s capture set whose classifier is Control or a descendant of Control. Non-control capabilities captured by the closure (e.g., file handles) are excluded from the result type, reflecting the fact that Try does not propagate them.

## 2.3 Case Study: Future[T] Cannot Handle Thread-Locals

Future[T] [47] represents a computation that may execute on an arbitrary worker thread. Because the task scheduler is free to migrate the computation between carrier threads, the closure submitted to a Future must not rely on any thread-local state. Thread-local resources include thread-local storage, local stack manipulation (Control capabilities, coroutines), and native C interop.

With classifiers, this restriction is expressed directly in the Future constructor:

```

object Future:
  def apply[T](body: () -> {any.except[ThreadLocal]} T): Future[T]^(body)

```

The .except[ThreadLocal] projection removes any capability whose classifier falls under ThreadLocal. Crucially, because exception handling is tied to the thread-local call stack, Control is defined as a child of ThreadLocal, so .except[ThreadLocal] excludes Control capabilities as well. This illustrates

| $x, y, z$                         | Variable          | $s, t, u :=$                                         | Term                | $B :=$               | Capability Bound |
|-----------------------------------|-------------------|------------------------------------------------------|---------------------|----------------------|------------------|
| $c$                               | Capture Variable  | $x$                                                  | variable            | $\phi$               | kind             |
| $k, l \in \mathcal{K}$            | Classifier Trait  | $v$                                                  | value               | $C$                  | capture set      |
| $\phi :=$                         | Classifier Kind   | $x y$                                                | application         | $E, F :=$            | Existential Type |
| $\emptyset$                       | empty             | $x[S]$                                               | type application    | $\exists c : B . T$  | existential      |
| $k - \bar{k}_i$                   | subtree           | $x[c]$                                               | capture application | $T$                  | type             |
| $\phi \vee \phi$                  | union             | $\text{let } x = t \text{ in } u$                    | let                 | $T, U :=$            | Type             |
| $\pi :=$                          | Projected Capture | $\text{let } \langle c, x \rangle = t \text{ in } u$ | existential let     | $S \wedge C$         | capturing        |
| $(\theta \mid \phi)$              | projection        | $v :=$                                               | Value               | $S$                  | pure             |
| $C, D := \{\pi_1, \dots, \pi_n\}$ | Capture Set       | $\lambda \ C (x : T) t$                              | function            | $R, S :=$            | Shape Type       |
| $\Gamma :=$                       | Context           | $\lambda \ C [X <: S] t$                             | type function       | $\top$               | top              |
| $\emptyset$                       | empty             | $\lambda \ C [c : B] t$                              | capture function    | $X$                  | type variable    |
| $\Gamma, x : T$                   | term binding      | $\text{pack } \langle C, x \rangle$                  | pack                | $\forall (x : T) E$  | function         |
| $\Gamma, X <: S$                  | type binding      | $\theta :=$                                          | Capture             | $\forall [X <: S] E$ | type function    |
| $\Gamma, c : B$                   | capture binding   | $x$                                                  | variable            | $\forall [c : B] E$  | capture function |
|                                   |                   | $c$                                                  | capture variable    |                      |                  |

Fig. 3. Abstract syntax of System Capless( $\mathcal{K}$ ). Changes compared to System Capless [60] are marked .

how the tree structure pays off: a single exclusion of an ancestor classifier automatically covers all of its descendants, without requiring the programmer to enumerate them.

Beyond these standard-library examples, Lutze et al. [24] have demonstrated the practical value of effect exclusions in existing code. We revisit such patterns in Section 6.2.

### 3 System Capless( $\mathcal{K}$ ): Capture Checking with Classifiers

We formalize capability classifiers in System Capless( $\mathcal{K}$ ). Our work is built upon System Capless [60], a core calculus for capture checking. It models a lambda calculus that tracks capabilities in types. The calculus follows monadic normal form (MNF) [14], where intermediate computations are bound by let expressions, and both functions and their arguments are restricted to variables. This does not reduce expressiveness: any application  $t u$  can be rewritten as  $\text{let } x_1 = t \text{ in let } x_2 = u \text{ in } x_1 x_2$ . Types are stratified into *shape types*  $S$  (function types, type variables,  $\top$ ) and *capturing types*  $T$ , which pair a shape type with a *capture set*. Existential types  $\exists c. T$  allow existentially quantifying a capture set, enabling abstraction over unknown capabilities. The calculus supports three forms of polymorphism: term abstraction over values, type abstraction over type variables bounded by shape types, and capture abstraction over capture variables bounded by capture sets. For example, we can type the original  $\text{Try}[\top]$  constructor using System Capless as follows:

$$\text{Try.apply} : \forall [T <: \top] \forall [c : *] \forall (\text{body} : (\forall (u : \text{unit}) T) \wedge \{c\}) \text{Try}[T] \wedge \{\}$$

The constructor is polymorphic in the body's return type  $T$ , and in its capture set  $c$ . The  $*$  bound indicates that the capture set is unbounded: the body can capture any variables in scope. The return type  $\text{Try}[T] \wedge \{\}$  indicates that the resulting  $\text{Try}[\top]$  has no captures, which is incorrect as previously mentioned. We will see how this is correctly typed in System Capless( $\mathcal{K}$ ) in the next section.

**Capture Kinding**

$$\boxed{\Gamma \vdash C : \phi}$$

$$\begin{array}{c} \frac{x : S^{\wedge} C \in \Gamma \quad \Gamma \vdash C.\text{proj}[\phi_1] : \phi_2}{\Gamma \vdash \{(x \mid \phi_1)\} : \phi_2} \quad (\text{K-VAR}) \\ \frac{\Gamma \vdash C : \phi \quad \phi \preceq \phi'}{\Gamma \vdash C : \phi'} \quad (\text{K-SUB}) \\ \frac{c : C \in \Gamma \quad \Gamma \vdash C.\text{proj}[\phi_1] : \phi_2}{\Gamma \vdash \{(c \mid \phi_1)\} : \phi_2} \quad (\text{K-CVAR}) \\ \frac{c : \phi_1 \in \Gamma}{\Gamma \vdash \{(c \mid \phi_2)\} : \phi_1 \wedge \phi_2} \quad (\text{K-CBOUND}) \\ \frac{\Gamma \vdash C_1 : \phi \quad \Gamma \vdash C_2 : \phi}{\Gamma \vdash C_1 \cup C_2 : \phi} \quad (\text{K-UNION}) \\ \frac{\phi \text{ empty}}{\Gamma \vdash \{(\theta \mid \phi)\} : \phi'} \quad (\text{K-ABSURD}) \\ \Gamma \vdash \{\} : \phi \quad (\text{K-EMPTY}) \end{array}$$

**Capture Subsetting**

$$\boxed{C_1 \sqsubseteq C_2}$$

$$\begin{array}{c} \frac{C_1 \sqsubseteq C_2}{C_1 \sqsubseteq C_2} \quad (\text{S-ELEM}) \\ \frac{\phi_1 \preceq \phi_2}{\{(\theta \mid \phi_1)\} \sqsubseteq \{(\theta \mid \phi_2)\}} \quad (\text{S-SUBKIND}) \\ \frac{\phi \text{ empty}}{\{(\theta \mid \phi)\} \sqsubseteq \{\}} \quad (\text{S-ABSURD}) \\ \{(\theta \mid (\phi_1 \vee \phi_2))\} \sqsubseteq \{(\theta \mid \phi_1), (\theta \mid \phi_2)\} \quad (\text{S-MERGE}) \end{array}$$

**Subcapturing**

$$\boxed{\Gamma \vdash C_1 <: C_2}$$

(changed rules; full set in the extended report [37])

$$\begin{array}{c} \frac{x : S^{\wedge} C \in \Gamma}{\Gamma \vdash \{(x \mid \phi)\} <: C.\text{proj}[\phi]} \quad (\text{SC-VAR}) \\ \frac{c : C \in \Gamma}{\Gamma \vdash \{(c \mid \phi)\} <: C.\text{proj}[\phi]} \quad (\text{SC-BOUND}) \\ \frac{C_1 \sqsubseteq C_2}{\Gamma \vdash C_1 <: C_2} \quad (\text{SC-ELEM}) \\ \frac{\Gamma \vdash C : \phi}{\Gamma \vdash C <: C.\text{proj}[\phi]} \quad (\text{SC-PROJ}) \end{array}$$

**Bound Subtyping**

$$\boxed{\Gamma \vdash B_1 <:_B B_2}$$

$$\begin{array}{c} \frac{\Gamma \vdash C_1 <: C_2}{\Gamma \vdash C_1 <:_B C_2} \quad (\text{B-SET}) \\ \frac{\phi_1 \preceq \phi_2}{\Gamma \vdash \phi_1 <:_B \phi_2} \quad (\text{B-KIND}) \\ \frac{\Gamma \vdash C : \phi}{\Gamma \vdash C <:_B \phi} \quad (\text{B-SET-KIND}) \end{array}$$

**Typing**

$$\boxed{C; \Gamma \vdash t : E}$$

(selected rules; full set in the extended report [37])

$$\begin{array}{c} \frac{x : S^{\wedge} C \in \Gamma}{\{x\}; \Gamma \vdash x : S^{\wedge} \{x\}} \quad (\text{VAR}) \\ \frac{C'; \Gamma \vdash x : (\forall (z : T) E)^{\wedge} C}{C'; \Gamma \vdash x y : [y/z] E} \quad (\text{APP}) \\ \frac{C; \Gamma \vdash t : T \quad C; (\Gamma, x : T) \vdash u : E}{\Gamma \vdash C, E \text{ wf}} \quad (\text{LET}) \\ \frac{C \uplus \{x\}; (\Gamma, x : T) \vdash t : E}{\{x\}; \Gamma \vdash \lambda^C (x : T) t : (\forall (x : T) E)^{\wedge} C} \quad (\text{ABS}) \\ \frac{C; \Gamma \vdash x : [D/c] T}{\Gamma \vdash D <:_B B} \quad (\text{PACK}) \\ \frac{C; \Gamma \vdash t : \exists c : B . T \quad \Gamma \vdash C, F \text{ wf}}{C; (\Gamma, c : B, x : T) \vdash u : F} \quad (\text{LET-E}) \end{array}$$

**Subtyping**

$$\boxed{\Gamma \vdash E_1 <: E_2}$$

(selected rules; full set in the extended report [37])

$$\begin{array}{c} \frac{\Gamma \vdash S_1 <: S_2 \quad \Gamma \vdash C_1 <: C_2}{\Gamma \vdash S_1^{\wedge} C_1 <: S_2^{\wedge} C_2} \quad (\text{CAPT}) \\ \frac{(\Gamma, c : B_1) \vdash T_1 <: T_2 \quad \Gamma \vdash B_1 <:_B B_2}{\Gamma \vdash \exists c : B_1 . T_1 <: \exists c : B_2 . T_2} \quad (\text{EXIST}) \end{array}$$

Fig. 4. Type system of System Capless( $\mathcal{K}$ ) (condensed). Changes from System Capless [60] are marked. The full rules can be found in the extended report [37].

|                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                                                        |
|-------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------|
| <b>Intersection</b>           | $\boxed{\phi_1 \wedge \phi_2 = \phi}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | (selected rules; full set in the extended report [37]) |
|                               | $\frac{k_1 \sqsubseteq k_2}{(k_1 - \bar{l}_1) \wedge (k_2 - \bar{l}_2) = k_1 - (\bar{l}_1, \bar{l}_2)} \quad \text{(I-SUBTREE-L)}$ $\frac{k_1 \perp k_2}{(k_1 - \bar{l}_1) \wedge (k_2 - \bar{l}_2) = \emptyset} \quad \text{(I-DISJOINT)}$ $\frac{\phi \wedge \phi_1 = R_1 \quad \phi \wedge \phi_2 = R_2}{\phi \wedge (\phi_1 \vee \phi_2) = R_1 \vee R_2} \quad \text{(I-UNION-R)}$                                                                                                                                                                                                                                                                |                                                        |
| <b>Subtraction</b>            | $\boxed{\phi_1 \setminus \phi_2 = \phi}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | (selected rules; full set in the extended report [37]) |
|                               | $(k_1 - \bar{l}_1) \setminus (k_2 - \epsilon) = k_1 - (k_2, \bar{l}_1) \quad \text{(ST-TREE)}$ $\frac{\phi_1 \setminus (k - \bar{k}_i) = R_1 \quad \phi_2 \setminus (k - \bar{k}_i) = R_2}{(\phi_1 \vee \phi_2) \setminus (k - \bar{k}_i) = R_1 \vee R_2} \quad \text{(ST-UNION-L)}$ $\frac{l \sqsubseteq k_2 \quad l \sqsubseteq k_1 \quad (k_1 - \bar{l}_1) \setminus (k_2 - \bar{l}_2) = \phi}{(k_1 - \bar{l}_1) \setminus (k_2 - (l, \bar{l}_2)) = (l - \bar{l}_1) \vee \phi} \quad \text{(ST-SUB-R)}$ $\frac{\phi \setminus \phi_1 = R_1 \quad R_1 \setminus \phi_2 = R_2}{\phi \setminus (\phi_1 \vee \phi_2) = R_2} \quad \text{(ST-UNION-R)}$ |                                                        |
| <b>Emptiness</b>              | $\boxed{\phi \text{ empty}}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                        |
|                               | $\emptyset \text{ empty} \quad \text{(E-EMPTY)}$ $\frac{k \sqsubseteq l_i}{k - (l_1, \dots, l_i, \dots, l_n) \text{ empty}} \quad \text{(E-ABSURD)}$ $\frac{\phi_1 \text{ empty} \quad \phi_2 \text{ empty}}{(\phi_1 \vee \phi_2) \text{ empty}} \quad \text{(E-UNION)}$                                                                                                                                                                                                                                                                                                                                                                              |                                                        |
| <b>Disjoint</b>               | $\boxed{\phi_1 \perp \phi_2}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Defined as $(\phi_1 \wedge \phi_2) \text{ empty}$ .    |
| <b>Subkinding</b>             | $\boxed{\phi_1 \preceq \phi_2}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | Defined as $(\phi_1 \setminus \phi_2) \text{ empty}$ . |
| <b>Inclusion</b>              | $\boxed{k \in \phi}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                                                        |
|                               | $\frac{k \sqsubseteq k_0}{k \in (k_0 - \epsilon)} \quad \text{(IN-BASE)}$ $\frac{k \not\sqsubseteq k_1 \quad k \in (k_0 - (k_2, \dots, k_n))}{k \in (k_0 - (k_1, \dots, k_n))} \quad \text{(IN-NONEXCL)}$ $\frac{k \in \phi_i}{k \in (\phi_1 \vee \dots \vee \phi_i \vee \dots \vee \phi_n)} \quad \text{(IN-UNION)}$                                                                                                                                                                                                                                                                                                                                 |                                                        |
| <b>Capture Set Projection</b> | $C.\text{proj}[\phi] := \{(\theta_i \mid \phi_i \wedge \phi)\} \text{ where } C = \{(\theta_i \mid \phi_i)\}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                        |
| <b>Exclusive Union</b>        | $C \uplus \{x_1, \dots, x_n\} = C \cup \{(x_1 \mid \top), \dots, (x_n \mid \top)\} \text{ where } \forall i, \phi. (x_i \mid \phi) \notin C$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                        |

Fig. 5. Kind Algebra of System Capless( $\mathcal{K}$ ) (condensed). The full rules can be found in the extended report [37].

The syntax and type system are presented in Figure 3 and Figure 4. Changes compared to System Capless are marked accordingly. System Capless( $\mathcal{K}$ ) is parameterized by a universe of classifiers  $\mathcal{K}$ , organized into a tree hierarchy. Each base capability and scoped capability can be tagged with one classifier. Captures are enhanced with *projections*, which are filters on classifiers based on a structure called a *classifier kind*.

### 3.1 Classifiers and Kinds

We embed the classifier tree  $\mathcal{K}$  into an infinite tree with root  $\top$ .  $k \sqsubseteq k'$  denotes that  $k'$  is an ancestor of  $k$  by standard tree relations. Naturally,  $k \sqsubseteq \top$  for all classifiers  $k$ . Furthermore, for any distinct classifiers  $k_1, k_2$ , we know that at most one of  $k_1 \sqsubseteq k_2$  and  $k_2 \sqsubseteq k_1$  holds. When neither is true, we say that  $k_1$  and  $k_2$  are *disjoint* (i.e., the subtrees rooted at  $k_1$  and  $k_2$  do not share any nodes).

Each node has a countably infinite number of children. This is crucial for modularity, as a classifier cannot be “singled out” by excluding all its known sub-classifiers: additional sub-classifiers can be added in another module, as in the following example:

## Semantic Domains

| $s, t, u := \dots$ | Term  | $\theta := \dots$                | Capture | $\Sigma :=$             | Label Context | $w :=$                           | Return Value |
|--------------------|-------|----------------------------------|---------|-------------------------|---------------|----------------------------------|--------------|
| $\ell$             | label | $\ell$                           | label   | $\emptyset$             | empty         | $v$                              | return       |
| $v := \dots$       | Value | $a := \langle \Sigma, w \rangle$ | Answer  | $\Sigma, \ell : S :: k$ | binding       | $\text{brk}(\ell, v)$            | break        |
| $\ell$             | label |                                  |         |                         |               | $F := \{\ell_1, \dots, \ell_n\}$ | Label Set    |

## Potential Use Set

 $\boxed{[v]}$ 

$$[\lambda^D(x : T)t] = D$$

$$[\lambda^D[X <: S]t] = D$$

$$[\lambda^D[c : B]t] = D$$

$$[\text{pack } \langle C, v \rangle] = \{\}$$

$$[\ell] = \{\ell\}$$

## Runtime Labels

 $\boxed{C_\Sigma^*}$  $\boxed{v_\Sigma^*}$ 

$$\emptyset_\Sigma^* = \emptyset$$

$$(C_1 \cup C_2)_\Sigma^* = (C_1)_\Sigma^* \cup (C_2)_\Sigma^*$$

$$\{(\theta \mid \phi)\}_\Sigma^* = \begin{cases} \{\ell\} & \theta = \ell, (\ell : S :: k) \in \Sigma \text{ and } k \in \phi \\ \emptyset & \text{otherwise} \end{cases}$$

$$v_\Sigma^* = [v]_\Sigma^*$$

## Big-step Evaluation (Selected)

 $\boxed{\Sigma \vdash t \Downarrow_F a}$ 

$$\frac{}{\Sigma \vdash v \Downarrow_F \langle \Sigma, v \rangle} \quad (\text{E-VAL})$$

$$\frac{\begin{array}{c} \Sigma \vdash t_1 \Downarrow_F \langle \Sigma', \lambda^D(x : T)t \rangle \quad \Sigma' \vdash t_2 \Downarrow_F \langle \Sigma'', v \rangle \\ D_{\Sigma''}^* \subseteq F \quad v_{\Sigma''}^* \subseteq F \\ \Sigma'' \vdash [[v]/x][v/x]t \Downarrow_{D_{\Sigma''}^* \cup v_{\Sigma''}^*} a \end{array}}{\Sigma \vdash t_1 t_2 \Downarrow_F a} \quad (\text{E-APP})$$

$$\frac{\begin{array}{c} \Sigma \vdash t \Downarrow_F \langle \Sigma', \lambda^D[X <: S_0]t \rangle \quad D_{\Sigma'}^* \subseteq F \\ \Sigma' \vdash [S/X]t \Downarrow_{D_{\Sigma'}^*} a \end{array}}{\Sigma \vdash t[S] \Downarrow_F a} \quad (\text{E-TAPP})$$

$$\frac{\begin{array}{c} \Sigma \vdash t \Downarrow_F \langle \Sigma', \lambda^D[c : B]t \rangle \quad D_{\Sigma'}^* \subseteq F \\ \Sigma' \vdash [C/c]t \Downarrow_{D_{\Sigma'}^*} a \end{array}}{\Sigma \vdash t[C] \Downarrow_F a} \quad (\text{E-CAPP})$$

$$\frac{\begin{array}{c} \Sigma \vdash t_1 \Downarrow_F \langle \Sigma', v \rangle \\ \Sigma' \vdash [[v]/x][v/x]t_2 \Downarrow_F a \end{array}}{\Sigma \vdash \text{let } x = t_1 \text{ in } t_2 \Downarrow_F a} \quad (\text{E-LET-V})$$

$$\frac{\begin{array}{c} \Sigma \vdash t_1 \Downarrow_F \langle \Sigma', \text{pack } \langle D, v \rangle \rangle \\ \Sigma' \vdash [D/c][[v]/x][v/x]t_2 \Downarrow_F a \end{array}}{\Sigma \vdash \text{let } \langle c, x \rangle = t_1 \text{ in } t_2 \Downarrow_F a} \quad (\text{E-EX-V})$$

$$\frac{\begin{array}{c} \Sigma \vdash t_1 \Downarrow_F \langle \Sigma', \ell \rangle \quad \Sigma' \vdash t_2 \Downarrow_F \langle \Sigma'', v \rangle \\ \ell \in F \end{array}}{\Sigma \vdash t_1 t_2 \Downarrow_F \langle \Sigma'', \text{brk}(\ell, v) \rangle} \quad (\text{E-BREAK})$$

$$\frac{\Sigma \vdash t_1 \Downarrow_F \langle \Sigma', \text{brk}(\ell, v) \rangle}{\Sigma \vdash t_1 t_2 \Downarrow_F \langle \Sigma', \text{brk}(\ell, v) \rangle} \quad (\text{E-APP-B1})$$

$$\frac{\Sigma \vdash t_1 \Downarrow_F \langle \Sigma', v_1 \rangle \quad \Sigma' \vdash t_2 \Downarrow_F \langle \Sigma'', \text{brk}(\ell, v) \rangle}{\Sigma \vdash t_1 t_2 \Downarrow_F \langle \Sigma'', \text{brk}(\ell, v) \rangle} \quad (\text{E-APP-B2})$$

Fig. 6. Checked big-step semantics of System Capless( $\mathcal{K}$ ): selected core rules. Remaining rules handle breaks in other constructs and can be found in the extended report [37].

```
// Module 1
trait A extends Classifier, SharedCapability
trait B extends Classifier, A // C likewise
def f(body: () -> {any.only[A].except[B].except[C]} Unit)
```

```
// Module 2, compiled separately
trait D extends Classifier, A
```

Function  $f$  cannot assume that no sub-classifier of  $A$  exists, since it can be arbitrarily extended by another module. Therefore, classifiers naturally avoid the closed-world problem presented by Lutze et al. [24]. Flix overcomes this problem by treating the effect set top as a symbolic constant during boolean unification, preventing negations from being translated into a finite positive set. In System Capless( $\mathcal{K}$ ), each subtree is assumed to have infinitely many children, so this cannot happen.

Kinds  $\phi$  represent filters for classifiers. To model `.only` and `.except`, we work with subtrees of classifiers when constructing kinds. They are represented as unions of “holed classifier subtrees”: a root subtree  $k_0$  and a list of excluded subtrees  $k_1, \dots, k_n$ . Each such subtree represents the set of all

classifiers  $k$  that are sub-classifiers of  $k_0$  but are *not* sub-classifiers of any remaining  $k_i$  (i.e.,  $k \sqsubseteq k_0$  and  $\forall i > 0, k \not\sqsubseteq k_i$ ). The inclusion relation ( $k \in \phi$ ) determines whether a classifier is included in a classifier kind. It is decidable, and is also used in the operational semantics.

We present in Figure 5 algorithmic rules for intersection ( $\phi_1 \wedge \phi_2$ ) and subtraction ( $\phi_1 \setminus \phi_2$ ) of kinds. The unambiguity of the rules depends on the previously mentioned sub-classifier-or-disjoint property of the classifier tree.

The intersection of two subtrees can simply be computed as a new subtree whose exclusion list contains both exclusion lists of the two inputs, and the new root is the deepest common classifier of the two input roots. This is the smaller root if they have a sub-classifier relationship (**I-SUBTREE-L**), or none if the roots are disjoint (**I-DISJOINT**). Compound cases are handled by computing the union of all intersections of pairs of subtrees.

Similarly, we handle subtraction of two subtrees individually, and compound cases are handled by the distribution on the left-hand side ( $\phi_1 \vee \phi_2 \setminus \phi = (\phi_1 \setminus \phi) \vee (\phi_2 \setminus \phi)$ ) (**ST-UNION-L**) and composition on the right-hand side ( $\phi \setminus (\phi_1 \vee \phi_2) = (\phi \setminus \phi_1) \setminus \phi_2$ ) (**ST-UNION-R**). For subtrees, we compute recursively on the exclusion list of the right-hand side. In the empty case (**ST-TREE**), we can simply append the root to the left-hand side's exclusion list. Otherwise, we follow the general equality of set subtractions  $A \setminus (B \setminus C) = (A \setminus B) \cup (A \cap B \cap C)$ . The rules (**ST-SUB-R**) and (**ST-IRREL-R**), (**ST-ABSURD-R**), (**ST-IRREL-L**), (**ST-SUB-L**) (found in the extended report [37]) handle each case based on the sub-classifier/disjointness relationship between the excluded node and the two roots.

Subkinding ( $\phi_1 \preceq \phi_2$ ) can be defined as empty subtraction ( $(\phi_1 \setminus \phi_2)$  **empty**), and disjointness of kinds can be defined as empty intersection. This is grounded in the fact that the subtraction operator satisfies the axioms of subtraction algebras [49, 15], which define an ordering relation.

There can be multiple representations of the empty set, so  $\phi$  **empty** is also defined algorithmically. The interesting case is when a subtree contains an ancestor node in its exclusion list (**E-ABSURD**).

We use a single classifier name to represent a subtree with the given classifier as root and no excluded roots, as well as a classifier kind containing that sole subtree. Following this notation,  $\top$  is the classifier kind containing all classifiers. The kind representing all classifiers except a subtree  $k$  can be written as  $\top - k$ .

The definitions of intersection and subtraction are equivalent to the set semantics. More details about the proofs can be found in Section 4.1.

### 3.2 Capability Projections

At the core of System Capless( $\mathcal{K}$ ) lie *projected captures* ( $\theta \mid \phi$ ). A projected capture consists of a capture  $\theta$ , applied to a classifier kind filter  $\phi$ . It represents *sub-parts* of  $\theta$  whose classifier  $k$  matches the kind  $\phi$  (i.e.,  $k \in \phi$ ). For instance, we can correctly type the signature of the  $\text{Try}[\top]$  constructor (previously mentioned in Section 2.2) in System Capless( $\mathcal{K}$ ) as

$$\text{Try.apply} : \forall [T <: \top] \forall [c : \top] \forall (\text{body} : (\forall (u : \text{unit}) T) \wedge \{c\}) \text{Try}[T] \wedge \{(c \mid \text{Control})\}$$

The return type captures a projection of the *body*'s capture set  $c$ , filtered to only the classifier subtree rooted at **Control**. The unbounded  $*$  is replaced with the  $\top$  kind bound, allowing all capture sets. Note that the capture set  $\{(c \mid \text{Control})\}$  is attached to the return type and not the function: the constructor is *pure* and does not capture any capabilities by itself.

For brevity we omit projections to  $\top$ . The notation  $C.\text{proj}[\phi]$  applies a further projection to each element in  $C$  by intersecting  $\phi$  with each singleton's existing projection, i.e.,

$$\{(\theta_1 \mid \phi_1), \dots, (\theta_n \mid \phi_n)\}.\text{proj}[\phi] = \{(\theta_1 \mid \phi_1 \wedge \phi), \dots, (\theta_n \mid \phi_n \wedge \phi)\}$$

Capture subsetting  $C_1 \sqsubseteq C_2$  follows normal subsetting rules  $C_1 \subseteq C_2$ , similar to System Capless [60], but is also extended to handle projections. A projected capture is smaller than the same

capture but with a super-kind (i.e., a coarser filter), by (**S-SUBKIND**). Projection to an empty kind is equivalent to removing that capture from the set (**S-ABSURD**). Finally, (**S-MERGE**) allows us to treat one capture projected to a union of two kinds as equivalent to two separate projected captures.

In System Capless, capture set variables can be either unbounded (as with the  $\text{Try}[T]$  example above) or bounded by other capture sets. System Capless( $\mathcal{K}$ ) replaces unbounded capture set variables with *kind-bounded* variables: they can only be instantiated with capture sets satisfying the given kind. For example, the constructor for  $\text{Future}[T]$  (Section 2.3), which forbids capabilities under  $\text{ThreadLocal}$ , can be typed as:

$$\text{Future.apply} : \forall[T <: \top] \forall[c : \top - \text{ThreadLocal}] \forall(\text{body} : (\forall(u : \text{unit}) T)^\wedge \{c\}) \text{Future}[T]^\wedge \{c\}$$

where the kind  $\top - \text{ThreadLocal}$  represents the kind of all classifiers, except the subtree rooted at  $\text{ThreadLocal}$ . The type system governs which capture sets can be instantiated under a kind bound through the *capture kinding* process described in the next section.

### 3.3 Capture Kinding and Subcapturing

Subcapturing rules  $C_1 <: C_2$  largely mirror those of System Capless. They follow the subsetting relation  $C_1 \sqsubseteq C_2$ , but with additional rules for term (**SC-VAR**) and capture variables (**SC-BOUND**), which refine captures based on their bounds. Projections on the variables are applied to the corresponding bound capture sets. The only new rule is (**SC-PROJ**), which allows us to equate any capture set  $C$  to its projected version  $C.\text{proj}[\phi]$ , if we can deduce that  $C$  contains only captures under kind  $\phi$ , through a judgment called *capture kinding*, which we shall describe below.

The capture kinding judgment  $\Gamma \vdash C : \phi$  is derived by looking up each projected capture in the context. For capture-set-bounded term and capture variables, we recursively check the definitions (in (**K-VAR**) and (**K-CVAR**)). Similar to subcapturing, projections of the capture are applied to the upper bound. For kind-bounded capture set variables in (**K-CBOUND**), the intersection of the projection and the kind bound is the most precise kind we can derive. Subkinding is handled by (**K-SUB**), with a special case for empty kinds in (**K-ABSURD**) to allow kinding judgments even on invalid references with empty projections.

Note that the simple addition of (**SC-PROJ**) allows us to derive useful, non-trivial facts. Projection preserves subcapturing ( $\Gamma \vdash C <: D$  implies  $\Gamma \vdash C.\text{proj}[\phi] <: D.\text{proj}[\phi]$ ) can be proven by induction on the original derivation, using composition of projections ( $C.\text{proj}[\phi_1].\text{proj}[\phi_2] = C.\text{proj}[\phi_1 \wedge \phi_2]$ ). Empty-kinded sets can be proven to be empty ( $\Gamma \vdash C : \phi$  where  $\phi$  **empty** implies  $\Gamma \vdash C <: \{\}$ ) by first projecting  $C$  to the empty kind  $\phi$  using (**SC-PROJ**), then using (**SC-ELEM**) to conclude  $\Gamma \vdash C.\text{proj}[\phi] <: \{\}$ , where the underlying subset relation is obtained by repeatedly applying (**S-ABSURD**) to each projected capture.

Together, kinding and subcapturing allow refinement and filtering of variables in capture sets. For example, with two disjoint child classifiers  $k_1, k_2 \sqsubseteq k$  and a kind-bounded capture set variable  $c : k_1$  in scope, we can derive that  $\{c\}.\text{proj}[k_2] <: \{\}$ , i.e., a function capturing values of kind  $k_2$  will not capture any capabilities of kind  $k_1$ .

### 3.4 Typing and Subtyping

Subtyping remains unchanged from System Capless [60]: subtyping of capturing types  $S_1^\wedge C_1 <: S_2^\wedge C_2$  requires both subtyping on the shape types and subcapturing on the capture sets (**CAPT**), but otherwise follows kernel System  $F_{\leq}$ , unsurprisingly. Capture set bound subtyping either follows subcapturing (when both bounds are capture sets), subkinding (when both bounds are kinds), or capture kinding when we refine a kind bound to a capture-set bound (**B-SET-KIND**).

Similar to System Capless, the typing judgment  $C; \Gamma \vdash t : E$  states that  $t$  has the existential type  $E$  under context  $\Gamma$  with the *use set*  $C$ . The use set represents capabilities that *may* be used during

the evaluation of  $t$ . We follow System Capless for use set judgments: values can be typed with an empty use set as they are already evaluated, variables are typed with themselves in the use set (**VAR**), and abstractions (**ABS**), (**TABS**), (**CABS**) reify the body's use set into the function's *capture set*, leaving an empty use set. Note that the use set is recorded in the lambda term, which is used in the checked big-step semantics (Section 3.6). Otherwise, typing is standard with regard to System  $F_{\leq}$ , and remains unchanged from System Capless. Note that let typing (**LET**) and (**LET-E**) require the final use set  $C$  and return types to be well-formed in the absence of the let-bound parameter, which we can achieve by widening its appearances in capture sets (e.g., by applying (**SC-VAR**)).

### 3.5 Translation from Surface Language

Scala provides **any** as syntactic sugar for the *universal capability*: a reference standing for “some unspecified capability in scope”. It does not appear in the formal calculus. Instead, **any** is *desugared* into explicit quantification over a fresh capture variable. In a *contravariant* input position, **any** introduces a fresh *capture abstraction*: the enclosing function becomes capture-polymorphic. In a *covariant* (output) position, **any** becomes an *existential type*. Consider the `Try.apply` constructor from Section 2.2:

```
def apply[T](body: () ->{any} T): Try[T]^{body.only[Control]}
```

The contravariant **any** on body's type introduces a fresh capture variable  $c : T$ . It is translated to:

$$\text{Try.apply} : \forall[T <: T] \forall[c : T] \forall(\text{body} : (\forall(u : \text{unit}) T) \wedge \{c\}) \text{Try}[T] \wedge \{(c \mid \text{Control})\}$$

The translation between the surface language and System Capless has been formalized in System Reacap [60], a surface calculus for capture checking with **any**, and applies directly to System Capless( $\mathcal{K}$ ). Section 5 describes the implementation.

### 3.6 Big-Step Semantics

We define *checked* big-step semantics in Figures 6 and 8. The judgment  $\Sigma \vdash t \Downarrow_F a$  includes access checks (in **green**) under label allowance  $F$ . The big-step evaluation involves a label context  $\Sigma$  that records the classifier and value type associated with created labels throughout the evaluation. Therefore, evaluation always returns a possibly-appended label context as part of its answer: either a return value  $\langle \Sigma', v \rangle$  or a propagating break  $\langle \Sigma', \text{brk}(\ell, v) \rangle$ .

Ignoring all access checks, the judgments ((**E-VAL**), (**E-APP**), (**E-TAPP**), (**E-CAPP**), (**E-LET-V**), (**E-EX-V**)) describe a standard top-level (i.e., no store bindings), substitution-based, call-by-value big-step reduction over the *relaxed*, direct-style syntax used in the proofs (Figure A.3 of the extended report [37]), since substitution takes evaluation out of MNF. Note that substituting a term variable  $x$  involves both a capture-set substitution  $[C/x]$  and a regular term substitution  $[v/x]$ , as  $x$  can appear in both contexts.

The access checks make the scoping discipline of labels explicit. The allowance  $F$  directly governs breaks: invoking a label (**E-BREAK**) is stuck if the label is not included in the allowance. At the outer typing-to-runtime boundary, the allowance is the runtime label set computed from the static typing capture set: it records only which labels may be accessed during evaluation, by comparing each label's projection kind to the current label context. Within the rules, allowances are otherwise ordinary runtime label sets. Intuitively, the runtime labels  $v_{\Sigma}^*$  (Figure 6) of a  $\lambda$ -abstraction are the set of labels that it can reach when its body is evaluated. Accordingly,  $\lambda$ -abstractions are entered under the label allowance dictated by their annotated capture sets.<sup>2</sup> Application rules ((**E-APP**), (**E-TAPP**), (**E-CAPP**)) check that the abstractions' and their arguments' runtime labels are bounded by

<sup>2</sup>We assume that  $\lambda$ -abstractions carry their annotated capture sets (cf. Figure 4).

the current allowance. This is what allows propagated breaks to stay well-scoped. All other rules support the *extended* System Capless( $\mathcal{K}$ ), which we describe in the next section.

### 3.7 Boundary, Break, and Intercept

To prove safety properties about the system (Section 4), we extend System Capless( $\mathcal{K}$ ) with three control-flow constructs (Figure 7): *boundary*, *break* (following [60, 5]), and a new construct *intercept*.

**Boundary and Break.** Following [60, 5],  $\text{boundary}[S, k]$  as  $\langle c, x \rangle$  in  $t$  introduces a scope with a fresh label  $\ell$ , which the body can use to transfer control (*break*) disruptively out of the scope. We extend this with a classifier  $k$ : the boundary rules ((E-BND-V), (E-BND-C), (E-BND-P)) create a fresh label with an arbitrary sub-classifier  $k_0 \sqsubseteq k$ . This non-determinism models the runtime class of a caught exception, which may be a concrete subclass of the declared one.

Breaks can be invoked by applying a label value  $l$  (of type  $\text{Break}[S]$ ) to the appropriate value  $v$  of type  $S$  ((E-BREAK) and statically (T-BREAK)), returning the disruptive answer  $\text{brk}(\ell, v)$ . This is propagated upwards, in a similar way to throwing exceptions (for example, as described by (E-APP-B1) and (E-APP-B2) for applications; other propagation rules can be found in the extended report [37]), until it is either caught by the corresponding boundary (E-BND-C) or an intercept (described below), or reaches the top level. Boundaries push the fresh label onto the persistent label context, but the label allowance includes it only during the evaluation of the body: the label may escape (e.g., inside returned abstractions), but invoking an escaped label is stuck. Corollary 4.3 proves that well-typed closed terms do not evaluate to  $\text{brk}$ .

**Intercept.** The construct  $\text{intercept}[S, C_t, \phi]$  with  $h$  in  $t$  intercepts any break that escapes  $t$  whose label has classifier  $k \in \phi$ , dispatching the caught label and its payload to the handler  $h$ . Evaluation is deterministic: a matching break is handled, a non-matching one propagates, and a normal return passes through unchanged ((E-ICP-M), (E-ICP-P), (E-ICP-V)). The inner term runs under the allowance of its annotated use set and may thus invoke more labels than the context allows, as long as they are caught: handlers are evaluated with the original allowance (E-ICP-M), while propagated labels are re-checked to be in the same allowance (E-ICP-P). Interestingly, we can refine the use set of the intercept expression: after handling labels of kind  $\phi$ , only captures outside  $\phi$  may escape from the body, together with the handler's own captures. Specifically, for handlers that *do not* re-throw (i.e., those that do not use the captured label), we can drop matching labels from the use set of  $t$ , so that only  $C_t.\text{proj}[\top \setminus \phi]$  is included (T-ICP-PASS).

The intercept construct acts as a modular extension to the extended System Capless [60]. It is a straightforward model for *intercepting* exception handlers: handlers that intercept an existing lexical exception handler, as in the case of Scala's interactions between  $\text{Try}[\top]$  [43] and *boundary* [46]. The separation is meaningful: it precisely defines the requirements that intercepting handlers must uphold to maintain *scope-safety*, without modifying the existing assumptions of lexical handlers.

**Encoding  $\text{Try}[\top]$ .** Scala's  $\text{Try}[\top]$  can be encoded into the extended System Capless( $\mathcal{K}$ ). Using Church encoding, we can represent the two cases of the container (a value of type  $\top$ , or a  $\text{brk}$  of an unknown type) as follows, where the extra capture-set parameter  $C$  represents the capture set of the  $\text{Try}$  value itself, to appear within parameter positions of the handlers:

$$\begin{aligned} \text{Try}(T, C) &= \forall[X <: \top]. \forall[c : \top]. \\ &\quad \left( \forall[s : (\forall(x:T) X) \wedge \{c\}]. \right. \\ &\quad \left. \forall[f : (\forall[Y <: \top]. \forall(b : (\text{Break}[Y]) \wedge C) (\forall(r:Y) X) \wedge \{c\}) \wedge \{c\}]. X \right) \wedge \{c : \top\} \cup C \end{aligned}$$

The constructor can then be encoded as taking a thunk  $b$ , running it under an intercept where  $\phi = \text{Control}$ , with the handler and final results wrapped accordingly into different cases of the

$\text{Try}(T, \{(b \mid \text{Control})\})$ . The full development in Lean 4 is further explained in Appendix B of the extended report [37].

## 4 Metatheory

We establish soundness of System Capless( $\mathcal{K}$ ) in three steps. First, the classifier kind algebra admits a set-theoretic semantics that justifies extensional reasoning about projections and handler dispatch. Second, unlike prior work on capture calculi [5, 60], which establishes soundness by small-step preservation and progress, we use a checked big-step semantics, a first in that line of work. This is useful for two reasons: (1) it makes the scoping discipline of labels explicit, and (2) it lets us reason directly about what values reach and how this relates to capture sets and classifiers. Third, we employ a standard safety proof for big-step semantics, with relaxed typing rules to handle direct-style, non-MNF terms, and an extension to answer typing that links returned breaks to label scoping, which allows us to show the relation between static typing capture/use sets and the usage of labels at runtime. The closest precedent is the second-class values literature [34, 56, 53], which also reasons in big-step style about what function values may capture, and logical-relations work on reachability types [2], which connects annotations to the values reachable at runtime. Neither qualifies types by classifier-indexed capture sets governed by subcapturing, nor tracks delimiter-scoped control. We sketch the most important aspects here and refer to the Lean mechanization [36] and Appendix B of the extended report [37] for the full development.

### 4.1 Set Semantics of Classifier Kinds

The kind algebra (Figure 5) admits a set-theoretic reading. Define  $\llbracket \phi \rrbracket = \{k \mid k \in \phi\}$ , where membership is the decidable inclusion judgment of Figure 5. Then intersection, subtraction, emptiness, sub-kinding, and disjointness correspond exactly to set intersection, difference, emptiness, inclusion, and disjointness. This lets us carry out later arguments about classifier projection, exclusion, and handler dispatch by ordinary set reasoning on kind denotations.

### 4.2 Runtime Relaxed Typing

Evaluation introduces labels and direct-style, non-MNF terms, which are not included in the original System Capless( $\mathcal{K}$ ) static typing. To reason about runtime terms, we introduce *relaxed typing* judgments  $\mathcal{C}; \Sigma; \Gamma \vdash_{\star} t : E$ , which are additionally parameterized by the label context and relax the MNF restrictions. Relaxed typing rules largely follow regular typing rules. We present the most interesting differences. The full set of rules can be found in the extended report [37].

The two judgments are connected by type-preserving translations to and from MNF: any typed MNF term  $(\mathcal{C}; \Gamma \vdash t : E)$  is relax-typed as is  $(\mathcal{C}; \Sigma; \Gamma \vdash_{\star} t : E)$ , and MNF normalization (Definition A.3 in the extended report [37]) maps any relax-typed term back to the original typing with label rules added  $(\mathcal{C}; \Sigma; \Gamma \vdash \hat{t} : E)$ . Therefore, relaxed typing works as a proof device: our safety theorem (Theorem 4.1) maintains relaxed typing as an invariant during evaluation, before re-normalizing the final result back into standard MNF typing.

**Typing Labels.** The rule (RT-LABEL) allows typing a label value present in the label context  $\Sigma$  at the corresponding Break  $[S]$  shape type. The interesting part lies in the capture set of the value: a label has a single classifier  $k$ , so it can be projected to any kind  $\phi$ , so long as it contains the classifier (i.e.,  $k \in \phi$ ). This is similarly presented in the additional capture kinding rules for labels, where (K-LABEL) allows kinding a (valid projection of a) label at any kind containing its classifier, while (K-LABEL-ABSURD) sees a projection outside of the label's classifier as the empty set. This allows us to freely change projections of a label within a capture set, as long as they remain valid, while retaining the accessibility of the label itself during computation of runtime labels.

## Syntax

 $s, t, u, h := \dots$ 
 $\text{boundary}[S, k] \text{ as } \langle c, x \rangle \text{ in } t$ 
 $\text{intercept}[R, C_t, \phi] \text{ with } h \text{ in } t$ 
 $R, S := \dots$ 
 $\text{Break}[S]$ 

## Term

 $\text{boundary}$ 
 $\text{intercept}$ 

## Shape Type

 $\text{break}$ 

## Subtyping

$$\boxed{\Gamma \vdash E_1 <: E_2}$$

$$\frac{\Gamma \vdash S_2 <: S_1}{\Gamma \vdash \text{Break}[S_1] <: \text{Break}[S_2]} \quad (\text{BREAK})$$

## Exception Handler Type Abbreviations

$$\text{Handler}_{\text{pass}}[E, \phi, C_h, C_t] := \forall [X <: T] \forall [c : C_t.\text{proj}[\phi]] \forall (b : \text{Break}[X] \wedge \{c\}) (\forall (y : X) E) \wedge C_h$$

$$\text{Handler}_{\text{gen}}[E, \phi, C_h, C_t] := \forall [X <: T] \forall [c : C_t.\text{proj}[\phi]] \forall (b : \text{Break}[X] \wedge \{c\}) (\forall (y : X) E) \wedge C_h \cup \{c\}$$

## Typing

$$\boxed{C; \Gamma \vdash t : E}$$

$$C; \Gamma \vdash x : \text{Break}[S] \wedge C_x$$

$$\frac{C; \Gamma \vdash y : S \quad \Gamma \vdash R \text{ wf}}{C; \Gamma \vdash x y : R}$$

(T-BREAK)

$$C_t; \Gamma \vdash t : E$$

$$\frac{C_h; \Gamma \vdash h : \text{Handler}_{\text{pass}}[E, \phi, C_h, C_t]}{C_t.\text{proj}[T \setminus \phi] \cup C_h; \Gamma \vdash \text{intercept}[E, C_t, \phi] \text{ with } h \text{ in } t : E} \quad (\text{T-ICP-PASS})$$

$$C \sqcup \{c, x\}; (\Gamma, c : k, x : \text{Break}[S] \wedge \{c\}) \vdash t : S$$

$$\Gamma \vdash S \text{ wf}$$

$$\frac{\Gamma \vdash S \text{ wf}}{C; \Gamma \vdash \text{boundary}[S, k] \text{ as } \langle c, x \rangle \text{ in } t : S} \quad (\text{T-BND})$$

$$C_t; \Gamma \vdash t : E$$

$$C_h; \Gamma \vdash h : \text{Handler}_{\text{gen}}[E, \phi, C_h, C_t]$$

$$\frac{C_t \cup C_h; \Gamma \vdash \text{intercept}[E, C_t, \phi] \text{ with } h \text{ in } t : E}{C_t \cup C_h; \Gamma \vdash \text{intercept}[E, C_t, \phi] \text{ with } h \text{ in } t : E} \quad (\text{T-ICP-GEN})$$

Fig. 7. Extended System Capless( $\mathcal{K}$ ) with boundaries and interceptions.

## Big-step Evaluation (continued)

$$\boxed{\Sigma \vdash t \Downarrow_F a}$$

$$\ell \text{ fresh} \quad k_0 \sqsubseteq k \quad t' = [\{\ell\}/c][\{\ell\}/x][\ell/x]t$$

$$\Sigma, \ell : S :: k_0 \vdash t' \Downarrow_{F \cup \{\ell\}} \langle \Sigma', v \rangle$$

$$\Sigma \vdash \text{boundary}[S, k] \text{ as } \langle c, x \rangle \text{ in } t \Downarrow_F \langle \Sigma', v \rangle$$

(E-BND-V)

$$\ell \text{ fresh} \quad k_0 \sqsubseteq k \quad t' = [\{\ell\}/c][\{\ell\}/x][\ell/x]t$$

$$\Sigma, \ell : S :: k_0 \vdash t' \Downarrow_{F \cup \{\ell\}} \langle \Sigma', \text{brk}(\ell, v) \rangle$$

$$\Sigma \vdash \text{boundary}[S, k] \text{ as } \langle c, x \rangle \text{ in } t \Downarrow_F \langle \Sigma', v \rangle$$

(E-BND-C)

$$\ell \text{ fresh} \quad k_0 \sqsubseteq k \quad t' = [\{\ell\}/c][\{\ell\}/x][\ell/x]t$$

$$\Sigma, \ell : S :: k_0 \vdash t' \Downarrow_{F \cup \{\ell\}} \langle \Sigma', \text{brk}(\ell', v) \rangle \quad \ell \neq \ell'$$

$$\Sigma \vdash \text{boundary}[S, k] \text{ as } \langle c, x \rangle \text{ in } t \Downarrow_F \langle \Sigma', \text{brk}(\ell', v) \rangle$$

(E-BND-P)

$$\Sigma \vdash t \Downarrow_{(C_t)_\Sigma^*} \langle \Sigma', v \rangle$$

$$\Sigma \vdash \text{intercept}[R, C_t, \phi] \text{ with } h \text{ in } t \Downarrow_F \langle \Sigma', v \rangle \quad (\text{E-ICP-V})$$

$$\Sigma \vdash t \Downarrow_{(C_t)_\Sigma^*} \langle \Sigma', \text{brk}(\ell, v) \rangle \quad (\ell : S :: k) \in \Sigma'$$

$$\frac{k \in \phi \quad \Sigma' \vdash h[S][\{(\ell | \phi)\}] \ell v \Downarrow_F a}{\Sigma \vdash \text{intercept}[R, C_t, \phi] \text{ with } h \text{ in } t \Downarrow_F a} \quad (\text{E-ICP-M})$$

$$\Sigma \vdash t \Downarrow_{(C_t)_\Sigma^*} \langle \Sigma', \text{brk}(\ell, v) \rangle \quad (\ell : S :: k) \in \Sigma'$$

$$k \notin \phi \quad \ell \in F$$

$$\Sigma \vdash \text{intercept}[R, C_t, \phi] \text{ with } h \text{ in } t \Downarrow_F \langle \Sigma', \text{brk}(\ell, v) \rangle \quad (\text{E-ICP-P})$$

Fig. 8. Checked big-step semantics of System Capless( $\mathcal{K}$ ): boundary and intercept rules.

**Non-MNF Terms.** Normal typing rules easily transfer to non-MNF terms: note that judgments such as  $D; \Gamma \vdash x : S \wedge C$  for variables can always be stated more precisely as  $\{x\}; \Gamma \vdash x : S \wedge C$ . We can always relax such premises into  $C; \Gamma \vdash t : S \wedge C$ , knowing that when  $x$  shows up in the use set, its value is being *used*, and so its *potential use set* (i.e., its annotated capture set during static typing) will be charged. There are, however, two exceptions requiring careful consideration: term application (**APP**) and packing (**PACK**). For application, we are more flexible about which capture set gets substituted into the dependent result type: while the original typing implicitly widens the argument variable's type to  $T$  and substitutes  $\{y\}$  for  $z$ , the relaxed rule makes the widening step

**Capture Kinding (for labels)**  $\boxed{\Sigma; \Gamma \vdash C : \phi}$

$$\frac{(\ell : S :: k) \in \Sigma \quad k \in \phi_l \quad k \in \phi}{\Sigma; \Gamma \vdash \{(\ell \mid \phi_l)\} : \phi} \text{ (K-LABEL)}$$

$$\frac{(\ell : S :: k) \in \Sigma \quad k \notin \phi_l}{\Sigma; \Gamma \vdash \{(\ell \mid \phi_l)\} : \emptyset} \text{ (K-LABEL-ABSURD)}$$

**Relaxed Typing (Selected Rules)**  $\boxed{C; \Sigma; \Gamma \vdash_\star t : E}$

$$\frac{(\ell : S :: k) \in \Sigma \quad k \in \phi}{\emptyset; \Sigma; \Gamma \vdash_\star \ell : \text{Break } [S]^\wedge \{(\ell \mid \phi)\}} \text{ (RT-LABEL)}$$

$$\frac{C'; \Sigma; \Gamma \vdash_\star x : [D/c]T \quad \Sigma; \Gamma \vdash D <_{\text{B}} B}{\emptyset; \Sigma; \Gamma \vdash_\star \text{pack } \langle D, x \rangle : \exists c : B.T} \text{ (RT-PACK-VAR)}$$

$$\frac{C_1; \Sigma; \Gamma \vdash_\star t_1 : (\forall (z : S^\wedge C_0) E)^\wedge C_1 \quad C_2; \Sigma; \Gamma \vdash_\star t_2 : S^\wedge C_2 \quad \Sigma; \Gamma \vdash C_2 < : C_0}{C_1 \cup C_2; \Sigma; \Gamma \vdash_\star t_1 t_2 : [C_2/z]E} \text{ (RT-APP)}$$

$$\frac{\emptyset; \Sigma; \Gamma \vdash_\star v : [D/c]T \quad \Sigma; \Gamma \vdash D <_{\text{B}} B}{\emptyset; \Sigma; \Gamma \vdash_\star \text{pack } \langle D, v \rangle : \exists c : B.T} \text{ (RT-PACK-VAL)}$$

**Answer Typing**  $\boxed{F; \Sigma; \Gamma \models_a w : E}$

$$\frac{\emptyset; \Sigma; \Gamma \vdash_\star v : E}{F; \Sigma; \Gamma \models_a v : E} \text{ (SA-RET)}$$

$$\frac{(\ell : S :: k) \in \Sigma \quad \ell \in F \quad \emptyset; \Sigma; \Gamma \vdash_\star v : S}{F; \Sigma; \Gamma \models_a \text{brk}(\ell, v) : E} \text{ (SA-BRK)}$$

Fig. 9. Capture Kinding for Labels, Relaxed typing definitions (selected rules) and Answer Typing rules used in the metatheory statements. The full relaxed typing judgments are given in the extended report [37].

explicit (RT-APP). For packing, generalizing to terms makes the calculus no longer call-by-value, so distinct rules for variable (RT-PACK-VAR) and value packing (RT-PACK-VAL) are introduced.

### 4.3 Main Results

The central result is safety of checked evaluation. Given a well-typed term under the top-level (i.e., empty) context and a label allowance of at least the runtime labels of the use set, evaluation never gets stuck and produces a well-typed answer in the result label context.

**THEOREM 4.1 (SAFETY OF CHECKED EVALUATION).** *If  $C; \Sigma; \emptyset \vdash t : E$  and  $C_\Sigma^* \subseteq F$  and  $\Sigma \vdash t \Downarrow_F^? a$ , then evaluation does not get stuck, and  $\exists w, \Sigma' \supseteq \Sigma$  such that  $a = \langle \Sigma', w \rangle$ , and  $F; \Sigma'; \emptyset \models_a w : E$ .*

where  $\Sigma \vdash t \Downarrow_F^? a$  means that evaluation terminates with answer  $a$  or gets stuck (i.e., it does not diverge)<sup>3</sup>. The proof proceeds by induction on the big-step derivation. The full development can be found in Appendix A of the extended report [37] and is mechanized in Lean 4 [36]. Note that in the case of returning a value, we immediately obtain type safety:

**COROLLARY 4.2 (TYPE SAFETY).** *If  $C; \Sigma; \emptyset \vdash t : E$  and  $C_\Sigma^* \subseteq F$  and  $\Sigma \vdash t \Downarrow_F \langle \Sigma', v \rangle$ , then  $\emptyset; \Sigma'; \emptyset \vdash_\star v : E$ . Equivalently,  $\emptyset; \Sigma'; \emptyset \vdash \widehat{v} : E$ .*

Furthermore, from the links between checked evaluation's label allowance and answer typing, we can derive additional properties about labels, breaks, and capture sets.

**COROLLARY 4.3 (EFFECT SAFETY).** *If  $\emptyset; \Sigma; \emptyset \vdash t : E$  and  $\Sigma \vdash t \Downarrow_\emptyset \langle \Sigma', w \rangle$ , then  $\exists v$  such that  $w = v$ .*

**COROLLARY 4.4 (USED LABEL PREDICTION).** *If  $C; \Sigma; \emptyset \vdash t : E$  and  $\Sigma \vdash t \Downarrow_{C_\Sigma^*}^? a$ , then evaluation does not get stuck.*

That is, evaluation of  $t$  relies only on access to runtime labels of  $C$ . In other words, the typing judgment's use set correctly predicts the set of labels used during evaluation of  $t$ .

<sup>3</sup>In the Lean 4 mechanization [36], big step evaluation is formalized as a fuel-based definitional interpreter, and non-divergence is defined by the interpreter terminating on finite fuel.

COROLLARY 4.5 (CAPTURE PREDICTION). *If  $D; \Sigma; \emptyset \vdash t : S \wedge C$  and  $\Sigma \vdash t \Downarrow_{D_\Sigma^*} \langle \Sigma', v \rangle$ , then*

$$\Sigma'; \emptyset \vdash [v] <: C \quad \text{and} \quad [v]_{\Sigma'}^* \subseteq C_{\Sigma'}^*$$

Recall that a potential use set  $[v]$  bounds the captures that a value reaches upon usage. We can predict the potential use set of the answer returned by the evaluation of a term from its static typing judgment. This is similar to the Capture Prediction for Terms lemma in  $CC_{<:\square}$  [5].

COROLLARY 4.6 (HANDLER COVERAGE). *If  $D; \Sigma; \Gamma \vdash t : E$  and  $\Sigma \vdash t \Downarrow_{D_\Sigma^*} \langle \Sigma', \text{brk}(\ell, v) \rangle$ , then*

- (1) break labels are within allowance:  $\ell \in D_{\Sigma'}^*$ .
- (2) matching labels are intercepted: *If  $t = \text{intercept}[R, C_t, \phi]$  with  $h$  in  $t'$ , and  $(\ell : S :: k) \in \Sigma$ , then either  $h$  was evaluated, or  $k \in T \setminus \phi$ .*

Type-level kind annotations thus predict both which labels may be reached by returned values and how `intercept` partitions propagating breaks into handled and escaping ones.

Two further consequences, found in Appendix A.5 of the extended report [37], clarify how the control operators behave. Fresh labels introduced by a boundary are local and never appear in the final answer. And for the pass rule of `intercept`, if the handler's own captures exclude labels of the intercepted kind, then no break whose classifier belongs to  $\phi$  can escape.

## 5 Implementation of Capability Classifiers in Scala

This section describes how the Scala 3 capture checker implements the classifiers of System Capless( $\mathcal{K}$ ) (Section 3), and how they fare in practice.

**Projections in Source Code.** The `.only` and `.except` projections of Section 2 map directly to the projected captures of Section 3. A chain of projections denotes a single subtree: `a.only[k1].except[l1]` stands for  $(a \mid (k_1 - l_1))$ . To project to a union of subtrees, the programmer writes a union of projected references:

$$\{a.\text{only}[k1].\text{except}[l1], a.\text{only}[k2].\text{except}[l2]\} \triangleq \{(a \mid (k_1 - l_1) \cup (k_2 - l_2))\}$$

During capture subsetting checks, the compiler compares a projected capture's kind against the union of the kinds of all projections of the same reference, by (S-MERGE).

**Declaring Classifiers.** Since classifiers are the plain traits of Section 2, the classifier tree of Section 3.1 is a slice of Scala's nominal subtype hierarchy, rooted at `Capability`, and the compiler answers sub-classifier queries by subtype tests. Scala traits allow multiple inheritance, so the compiler rejects any class that inherits two unrelated classifier traits, preserving the sub-classifier-or-disjoint property that Section 3.1 relies on.

**Representation in the Capture Checker.** The compiler retrofits classifiers onto the existing capture checker [60], whose data structures and constraint solver revolve around capture sets of references. Classifiers add one new form of reference, the counterpart of the projected captures  $\pi$  of Figure 3:

```
// x.only[o].except[e1]...except[en], the exclusions strictly below o
case class Classified(underlying: Capability, only: ClassSymbol, except: List[ClassSymbol]) extends DerivedCapability
```

A `Classified` reference represents the projected capture  $(x \mid (o - \bar{e}))$ . Its `only` and `except` fields form one holed subtree of Section 3.1. Kinds never appear as objects of their own, and solver and set operations carry over unchanged. The cost surfaces in coverage checking: a projection of `b` may be covered by no single reference and still be covered by several projections of `b` together. The checker decides such cases with the remainder computation of Figure 10, which subtracts each covering subtree from the covered one and accepts when nothing remains, deciding subkinding as emptiness of subtraction. Each branch implements one subtraction rule of Figure 5, named in its comment.

**Normal Forms and Subcapturing.** A smart constructor maintains the invariants noted in the comments of `Classified`: chained `.only` projections collapse to their least classifier, exclusions outside `only` drop, an exclusion covering `only` empties the whole reference (rules (`E-ABSURD`) and (`S-ABSURD`)), and the exclusion list stays pruned and sorted. The checker never meets a degenerate kind. Subcapturing  $\Gamma \vdash C_1 <: C_2$  then asks, for each reference in  $C_1$ , whether  $C_2$  accounts for it in one of three ways. A single reference subsumes it, following paths and variable bounds, rules (`SC-VAR`) and (`SC-BOUND`), and weakening the classifier by (`S-SUBKIND`). Several projections of the same reference cover it together, decided by the remainder computation of Figure 10, by rule (`S-MERGE`). Finally, the capture set of its type accounts for it recursively.

**Cost of the Kind Algebra.** Classifier comparisons are single subtype tests, and most kind operations are polynomial. Membership and emptiness reduce to linear scans, intersection and disjointness to the pairwise intersections of the two kinds' subtrees. The exception is subtraction, and with it subkinding. One call to the remainder computation of Figure 10 costs  $O(e)$  subtype tests for a subtrahend with  $e$  exclusions and returns at most  $e + 1$  subtrees, since the `st-sub-r` branch adds

```
// (o1 - e1) \ (o2 - e2), as a union of subtrees
type Subtree = (Cls, List[Cls])           // o - ē
def subtract(o1: Cls, e1: List[Cls],
            o2: Cls, e2: List[Cls]) =
  def go(ex: List[Cls]): List[Subtree] = ex match
    case Nil => (o1, o2 :: e1) :: Nil      // st-tree
    case l :: ls =>
      if !l.isSub(o2) then go(ls)          // st-irrel-r
      else if l.isSub(o1) then (l, e1) :: go(ls) // st-sub-r
      else if o1.isSub(l) then (o1, e1) :: Nil // st-sub-l
      else go(ls)                         // st-irrel-l
  go(e2).filterNot(isEmpty)
```

Fig. 10. The kind remainder computation, abridged. Comments name the subtraction rules of Figure 5.

one subtree per exclusion it meets. Subtracting a whole kind iterates the computation over its subtrees, so a kind with  $s$  subtrees can grow to  $O(s(e + 1)^n)$  subtrees under a subtrahend with  $n$ . In practice the exponent stays small: annotation kinds hold one or two subtrees, exclusion lists rarely go beyond a handful of classifiers, and the final `filterNot` of Figure 10 normalizes away empty subtrees. Accordingly, we observe no noticeable compile-time regression against the capture checker of System Capless, whose checking phase takes under 15% of total compilation time [60, Table 1]. A dedicated performance study across compiler and ecosystem is future work.

**Capability Classes.** Section 2 tags a class with a classifier through its `extends` clause. We call such classes *capability classes*:

```
class P(val q: Q^*) extends Control
```

Every instance of `P` is a capability classified under `Control` and enters capture sets as the projection `any.only[Control]`. The instance's captures must fit within that projection, so a classified class can hold only capabilities under its classifier. The field `q` above must therefore either have a `Control`-classified type `Q`, or constrain its capture set to a `Control` subset, as in `q: Q^{any.only[Control]}`. In exchange, clients may assume the tighter default: the shorthand `P^*` in parameter position stands for `P^{any.only[Control]}` rather than `P^{any}`. The declared classifier bounds the capabilities an instance holds rather than tagging them all exactly. Note that the classifier `Control` does not bound a class at *exactly* `Control`, but at the *subtree rooted at* `Control` (as the projection on `any` indicates). This looseness enables encapsulation: a class may keep private members at finer sub-classifiers, and clients can track those subsets (Section 6.3).

**Capture Inference.** Capture checking runs as its own phase after type checking and local type inference, solving subset constraints over capture set variables on the typed program [62, 60]. An inferred set contains the exact references a term uses, such as the path `file.read`, and never a projection. A projection such as `file.only[Read]` covers a whole subset of the capabilities

reachable through `file`, a coarser statement. Writing one is a deliberate widening, which belongs in annotations at API boundaries, in particular where the precise path is hidden (Section 6.3). Projections from annotations flow through the solver’s subset constraints like any other reference.

**Standard-Library Coverage.** By `tokei`’s count of non-comment, non-blank lines in sources compiled under capture checking, the standard library is 81.7% capture-checked (45,146 of 54,992 lines) once classifiers and the accompanying library changes are in place, up from 66.7% (36,605 of 54,841 lines) on the classifier-free Scala 3.8.0 baseline, which already incorporates System Capless. Classifiers do not account for the whole difference, but without them types such as `Try` and `Future` and their packages `scala.util` and `scala.concurrent` cannot be typed precisely at all. The annotation burden is small: typing these signatures precisely takes 14 `.only` and 151 `.except` projections across the whole library.

**Impact on Existing Code.** Adopting classifiers changes almost no existing capture-checked code. Fully polymorphic capture sets keep their meaning under the top classifier `Capability`, so the capture-checked collections of System Capless need no classifier-specific changes. The one source-level incompatibility concerns capability declarations. Scala seals `Capability`, so a user-defined capability must extend one of its two standard children of Section 2, `SharedCapability` or `ExclusiveCapability`. The latter is subjected to Scala’s tracking of exclusive capabilities [61], and classifiers enforce non-inclusion of such capabilities in a shared context. Sealing the root does not conflict with the open classifier tree of Section 3.1, which gives every classifier unboundedly many children. The checker never treats the two children as exhausting `Capability`: excluding both still leaves a nonempty kind.

## 6 Discussion

We discuss design decisions surrounding classifiers and their implementation.

### 6.1 Why a Tree of Classifiers?

**A separate kind.** Set-based [27] and boolean-algebraic [24, 9] effect systems can express a finite subset of effects, or the effect universe except a finite subset, but not an open specification: for example, `Control` capabilities include not only those defined in the standard library, but also an unbounded number of capabilities in other modules. By separating classifiers from capabilities, we provide a simple solution to classification: capabilities may tag themselves with new or existing classifiers, and the type system treats the set of capabilities in a particular classifier as unbounded.

We deliberately decouple capability classifiers from shape types for simplicity: classifiers have a much more rigid structure than types. This is reflected in System Capless( $\mathcal{K}$ ), where classifier and kind operations are algorithmic and total. Furthermore, this separation allows the core capture calculus to evolve mostly independently, since the integration surface is small (minor changes in subset calculation and one additional subcapturing rule). The Scala implementation also benefits from this restriction: a single-inheritance trait system for classifiers is simple to work with.

**The need for hierarchies.** A system with flat classifiers (i.e., no sub-classifiers) was also considered. However, classifiers tend to organize into hierarchies, especially permission classifiers such as `Read` and `ReadWrite` (Section 6.3). Flat classifiers would instead require multiple tags on a single capability, as in a tagging system where a read-write reference must carry separate read and write tags, placing a heavy burden on users to tag their capability classes. An open tree structure (or more flexible structures, e.g., lattices) models such hierarchies more naturally.

**Disjoint decompositions.** However, an open lattice is too flexible: we lose the ability to reason about disjointness. Two sub-lattices upper-bounded by  $A$  and  $B$  in an open lattice are

never disjoint, since a future module can always create a new classifier  $C$  directly under  $A$  and  $B$ . Disjointness is useful in practice: capability classes that split their aggregated capabilities into sub-groups need a way to guarantee that these groups are disjoint. For example, a Database capability may partition its usage by table, modeled as sub-classifiers of Database. Without disjointness, it is not possible to assert that `db.readUsers` uses `db.only[UserTable]` and not `db.only[TransactionTable]`.

```
trait Database extends Classifier, ExclusiveCapability
trait UserTable extends Classifier, Database
/* Similarly, TransactionTable, ProductTable ... */

class DBImpl extends Database:
  val readUsers: () -> {this.only[UserTable]} List[User]

// does not type check with a lattice!
val doesntTouchTransactions :
  () -> {db.except[TransactionTable]}
    List[User]
    = db.readUsers
```

Flix [24, 23] describes disjoint subsets with effect variables or associated effects, but disjointness must be requested explicitly. The Flix analogue of `readUsers` subtracts every sibling table from its effect, as in `List[User] \ {UserTable - TransactionTable - ProductTable}`. Boolean-algebraic subtyping faces the same problem: the effect parameter `UserTable` must be a subtype of the negation of all preceding parameters. InvalML [9] provides the outer scope variable  $\omega$  to refer to union of visible effect parameters in scope, but are limited to region variables specifically. A classifier tree approach enjoys disjointness by definition.

## 6.2 Fine-Grained Capability Classification on References

Lutze et al. [24] compile a set of real-world effect exclusion patterns. We successfully replicated all 59 case studies in Scala with classifiers. In this section, we show how classifiers enable fine-grained control over individual references that Flix's global exclusions cannot express.

**Simple effect exclusion.** Many patterns simply restrict a closure parameter from performing certain effects. We model this by creating a new classifier for the kind of effects to be disallowed. For instance, from the `amule` example<sup>3</sup>, we can model a function that must not invoke any `CSafeIOException`:

```
trait CSafeIOException extends Classifier, Control
case class CFileDataIO[T](doRead : (T, Long) -> {any.except[CSafeIOException]} Long)
```

In addition to preserving semantics, we can also mark `CSafeIOException` as part of `Control` capabilities, such that external code may properly reject usage of `C` exception handlers.

A more involved example comes from `dune`, where the `runWithErrHandler` function requires the body parameter `f` to not nest another `runWithErrHandler` call, and the handler function `handleErrNoRaise` may not raise exceptions. We capture the requirements by creating a classifier `ErrHandler` and giving it to the global capability `RunWithErrHandler` (Figure 11, left).

Here, `f` can throw any exceptions but cannot mention `RunWithErrHandler`, since it is under the `ErrHandler` classifier. Note, however, that the specification is ambiguous on whether `handleErrNoRaise` can use another error handler in its body. The declaration in Figure 11 disallows it (as `Control` is a parent of `ErrHandler`), but we can allow this by adding `any.only[ErrHandler]` (to allow all error handlers) into `handleErrNoRaise`'s capture set. Going further, we can allow *only* the same `RunWithErrHandler` mechanism to be used, by setting the capture set to `{this, any.except[Control]}`.

**Per-reference privilege restriction.** Where classifiers go beyond Flix is in restricting specific references rather than globally banning effect classes. Another example from Lutze et al. [24] highlights this: the `withTransaction` function from the `google-cloud-go` example<sup>4</sup> takes a closure with a `Transaction` as its input. This closure can use the `Transaction`, but *must not* call `commit` or `rollback`

<sup>4</sup>The original definitions can be found in [amule-project/amule](#) and [google/google-cloud-go](#) GitHub repositories.

```

trait ErrHandler extends Classifier, Control

object RunWithErrHandler extends ErrHandler:
  type Fiber[_] // threaded computation
  type Raise    // exception-raising capability
  def apply[A](
    /* f must not create ErrHandlers */
    f: this.Raise ->{any.except[ErrHandler]} A,
    /* cannot use exceptions */
    handleErrNoRaise: Exception ->
      {any.except[Control]} Fiber[Unit],
  ): Fiber[A]

trait Commit extends Classifier, SharedCapability
trait Rollback extends Classifier, SharedCapability

trait Transaction:
  val commit: () ->{this.only[Commit]} Unit
  val rollback: () ->{this.only[Rollback]} Unit
  /* other operations... */

  // runs body with the transaction, commit on end
  def withTransaction[T, E^](
    body: (tx: Transaction^>) ->
      (() ->{E, tx.except[Commit].except[Rollback]} T)): T

```

Fig. 11. Effect exclusion in real-world APIs: RunWithErrHandler from dune (left) and withTransaction from google-cloud-go (right).

```

/* User-defined capability classifiers */
trait ReadWrite extends Classifier, SharedCapability
trait Read extends Classifier, ReadWrite

trait File(val name: String):
  // capability members, ensured to be erased
  erased val r: Read^
  erased val rw: ReadWrite^

  // operations guarded by capability members
  val read: () ->{r} Int
  val write: Int ->{rw} Unit

  // runs f with an open file, closes it after use
  def withFile[T](f: File^ => T): T

```

(a)

```

class List[+T]:
  def parMap[U](f: T ->{any.only[Read]} U): List[U]

  withFile: file =>
    val list = List(99,97,112,121,98,97,114,97)
    list.parMap: item =>
      file.read() // ok
      file.write(42) // error: capturing ReadWrite

```

(b)

```

trait File(val name: String):
  erased private val r: Read^
  erased private val rw: ReadWrite^
  val read: () ->{this.only[Read]} Int
  val write: Int ->{this.only[ReadWrite]} Unit

```

(c)

Fig. 12. Read-only parallel map: (a) capability declarations, (b) their use, and (c) with members encapsulated.

on it. The Flix implementation solves this by completely banning usage of *all* Commit and Rollback effects, which is too conservative. By precisely projecting the transaction's identity in the capture set, we can do better (Figure 11, right). The withTransaction function accepts a closure that takes a Transaction, and then *captures* a limited variant of this transaction in its output closure. Note that the parameter closure itself is *pure*: it has no capture set, meaning it does not perform any operations on its own other than pure computation. The *returned* function value however may use tx, but not its Commit nor Rollback subset. Interestingly, by having a capture variable E in its captures, it can use other capabilities, including Commit/Rollback capabilities of *other* transactions. Note that E is defined outside of tx's scope, so it cannot contain tx.

### 6.3 Constraining Between Levels of Classifiers

Beyond exclusions on different classifiers, the flexibility of classifiers allows us to express complex restrictions between levels of classifiers. We present an example from Osvald et al. [34], which was also posed as a challenge for capture-checking systems in [56]. In this example, we have a parallel map operation on a List data structure that should not perform any write operations, as non-deterministic writes are one of the most common sources of data races. On the other hand, non-deterministic reads are safe in the absence of writes.

We introduce two new classifiers (Figure 12) Read and ReadWrite, with the former a sub-classifier of the latter. Each File now holds two compile-time-only capabilities corresponding to these classifiers,

```

def logErrors(f: () => Unit): Unit =
  try
    f()
  catch case (exc: Exception)
    (using ct: CanThrow[exc.type]^) =>
      println(exc.toString())
      throw exc // intercept & rethrow

case class Failure(e: Exception, ct: CanThrow[e.type]^)
def captureException(f: () => Unit)
  : Option[Failure^{f.only[Control]}] =
  try
    f(); None
  catch case (exc: Exception)
    (using ct: CanThrow[exc.type]^) =>
      Some(Failure(exc, ct)) // store exc and its CanThrow!

```

Fig. 13. Intercepting handlers: `logErrors` rethrows the caught exception (left), `captureException` stores it together with its `CanThrow` capability (right).

and operations on the file now capture these capabilities. Note that calling these operations will “use” the capability that was captured.

When type-checking the closure passed into `parMap`, the presence of the `file.rw` capability causes the compiler to reject the call, due to the capture set `{file.r, file.rw}` not satisfying the capture kind `Read`. On the other hand, without the `file.write` call, the example would compile.

We can go further and encapsulate the compile-time capabilities (Figure 12c), using `this.only[Read]` to refer to the subset of the `File` itself that contains only `Read` capabilities. The compiler guarantees that the `File` implementation will not capture `rw` in `read`. We however gain a clearer public API, free of the “administrative” capabilities of the implementation. On the other hand, `parMap` should also be more permissive with capabilities that are *neither* reading or writing to references. Depending on API considerations, they can be allowed by including `any.except[ReadWrite]` in `f`’s capture set.

#### 6.4 Non-Lexical Exceptions with Lexical Effect Handlers

Capture checking calculi [5, 60] promote lexical effect handling, where scoped effects like exceptions [32] are assumed to be handled by tunneling [64]. This is, however, not the case for exception handling on the JVM [65] or JavaScript, two main compilation targets for Scala. To maintain compatibility with these exception semantics, we can extend the `CanThrow` model to allow *intercepting* handlers by including the `CanThrow` capability as part of the thrown exception. Any `catch` clause can then rethrow the same exception type as the caught exception, while effect safety is retained.

In Figure 13 (left), `logErrors` prints exceptions thrown by `f` and then rethrows them. Note that apart from those captured by `f`, `logErrors` does not require any additional capabilities: exception safety is retained even when we rethrow the exception, since a handler for it is already known to exist. The `CanThrow` capability has the singleton type of `exc`, because the tested type `Exception` is too coarse: the original exception handler may not handle a different subtype of `Exception`.

One question remains: what if we were to *store* this capability? In Figure 13 (right), `captureException` *stores* the `CanThrow` capability and returns it, allowing the caller to unpack the capability and rethrow the exception. What does the resulting `Failure` capture? Classifiers provide a solution: since `CanThrow` capabilities have the `Control` classifier, we can filter the capture set down to `f.only[Control]`, which contains all possible `CanThrow` capabilities.<sup>5</sup>

#### 6.5 Classifiers as Traits

The classifier universe presented in this paper is distinct from types for pragmatic reasons. However, in the Scala implementation, classifiers are simple traits. While they are restricted, we can still leverage this fact to impose additional constraints on implementing capabilities.

<sup>5</sup>An astute reader may recognize that this is the same situation as `Try[T]` in Section 2: this is exactly the reasoning behind the capture sets for its constructor.

Scala's `Unscoped` classifier is one such example: it represents capabilities that are self-contained and can be returned from a scope, such as owned, mutable data structures. The class restriction requires all `Unscoped` values to capture only other `Unscoped` values. This allows the compiler, with uniqueness tracking [61], to safely treat returned `Unscoped` values as completely fresh, enabling capabilities to be tracked in a non-scoped way. Formalizing this extension is future work.

As another example, serializable closures require all their captures to also be serializable. Spores [29] track this in Scala by strictly controlling captured variables through a DSL implemented as Scala macros, forcing the user to declare all captures in advance. With classifiers, we can fuse the serializability requirement and functionality into a single classifier trait:

```
trait Serializable extends Classifier, SharedCapability:
  def serialize(): Array[Byte]
  def deserialize(from: Array[Byte])
class Spore(inner: () ->{any.only[Serializable]} Unit)
```

The `Spore` class accepts closures that capture only serializable references. The compiler can then use this information to safely derive serialization methods for such closures, while the usage of spores remains simple and expressive: they are still ordinary function types.

## 6.6 Limitations

Classifiers rely on subkinding alone, with no kind variables, so the system cannot constrain two unknown capture sets to be disjoint, e.g., a parallel combinator quantifies over two capture variables,

```
def fork[A, B, E1^, E2^](f: () ->{E1} A, g: () ->{E2} B): (A, B)
```

but no bound makes  $E1$  and  $E2$  disjoint, so `fork` cannot promise non-interference. Flix [24] states this disjointness with effect differences  $p1: T \setminus \{e1 - e2\}$ ,  $p2: U \setminus \{e2 - e1\}$ . InvalML [9] states it as a negation bound  $\beta \leq \neg\alpha$  between quantified effect variables, which transposed to our setting would be a capture-set bound  $E2 \leq \neg E1$ , negating sets of references rather than kinds. Capture checking addresses non-interference through an orthogonal separation mechanism instead, formalized in System Cpybara [61] and shipped as Scala's separation checking [48].

The kind algebra checks given kinds and never solves for an unknown one. In Flix, passing an `IO` function to a parameter of effect `ef - Throw` makes boolean unification derive `ef` from `IO = ef - Throw`. Our checking never needs such a step, since a call site requires some instantiation below its bound rather than a most general solution, and capture inference finds the least one. Every exclusion pattern of Section 6.2 type-checks this way. The difference surfaces only at API boundaries, where projections must be written by hand because inference never produces them (Section 5).

Being subtree-based, classifier kinds don't have non-trivial meets: two sibling subtrees always meet at an empty kind. Therefore, a capability cannot be classified at two sibling classifiers: The compiler rejects `class Log extends Read, Serializable outright` (Section 5), and requiring `.only[Read]` and `.only[Serializable]` on a capture set collapses it to empty. Qualifier lattices have exact meets: in System  $F_{\leq}^Q$  [18], variables can be quantified as  $l_1 \wedge l_2$  where  $l_1, l_2$  are both base lattice elements (corresponding to a single classifier), and can admit both declarations. Neither algebra subsumes the other: the tree lacks meets, but enjoys complements and disjoint decompositions.

## 7 Related Work

**Capability-based Effects.** Type-and-effect systems date back to Lucassen and Gifford's polymorphic effects [22]. Craig et al. [8] show that capabilities can be tracked in a type system to ensure capability safety and reason about effects. Brachthäuser et al. [7] view effect types as capabilities required from the calling context, enabling lightweight effect polymorphism without

effect variables, while coeffect systems [35] study contextual requirements more generally. This perspective is close to capture tracking, since a capture set records which capabilities a term requires from its environment. Capture calculus [5, 60, 59] tracks captured capabilities in Scala types, and our calculus builds directly on Xu et al. [60]. Tang and Lindley [50] give a uniform encoding of row-based and capability-based systems into modal effect types.

Capture checking is more than a lightweight effect system. A capture set names program values, often paths such as `body`, `tx`, or `file.r`, so capture checking itself reasons about capabilities by the identity of the values that carry them, keeping two file handles `file1` and `file2` distinct. Classifiers inherit this precision: a projection like `tx.except[Commit]` restricts one particular transaction rather than a whole effect class (Sections 6.2 and 6.3). The same capturing-types discipline reaches further, to sharing, lifetimes, aliasing, and separation of resources [59, 61], which traditional effect systems do not track directly. TACIT builds agent security on the purity of empty capture sets [33].

**Effect Classification and Exclusions.** Flix [24] introduces effect exclusion on a boolean algebra of effect sets, typing functions that accept any effects *except* a given set, with full Hindley-Milner inference by boolean unification. Checking there is equality-based, ours subsumption-based [52, 54]. Boolean unification keeps the top of the algebra symbolic to stay sound in an open world, and the classifier tree keeps the top of every subtree symbolic (Section 6.1). We replicate Flix’s case studies in Section 6.2, and Section 6.6 states what Flix can express that classifiers cannot.

Boolean-algebraic type-and-effect systems in general incorporate intersection and negation into effect typing [26, 9]. They are more expressive than our system because they allow effect set variables in algebraic expressions, but also considerably more complex. Classifiers can also represent exclusion of open sets of classifiers, which does not appear to be representable with intersection and negation of finite sets.

Row typing offers another route to classifying and filtering effects. Rémy’s record calculus attaches presence and absence flags to row labels [40], and the Rose language of Morris and McKinna [31] derives absence and disjointness from qualified predicates over rows, so both can state that a named label is absent even from an otherwise open row. Neither calculus, as defined, can state absence of an open category: a row is a finite list of named labels over one uniform tail, so it can mark finitely many labels absent or close the remainder entirely, but cannot exclude a whole open-ended category while leaving the rest open. That is what `any.except[Control]` expresses, excluding the `Control` subtree together with every sub-classifier that later modules add. Rows could recover this by kinding the label universe into categories, which rebuilds the classifier tree on the label side. The modal encoding of Tang and Lindley [50] discussed above suggests a formal bridge between rows and capabilities.

Effect masking [4, 21, 19, 55, 51] provides a way to skip a certain effect handler at runtime when multiple handlers are installed. Biernacki et al. [4] formalize related selective forwarding via a lift operator in a logical-relations semantics of handlers, and Eff [3], Koka [19, 20], Frank [21], and scoped handlers [55] study handlers over open effect rows. Masking and lifting re-route the search for the nearest handler, whereas classifier projections subtract categories from what a reference may reach. Our `intercept` construct is where the two perspectives meet: it lets lexically scoped boundary/break control temporarily take on nearest-handler semantics, intercepting matching breaks, while the intercepted label’s capture set still governs where that label may be retained and used.

First-class names [57] distinguish scoped effect instances by explicit names, a complement to classifiers, which group capabilities into extensible semantic categories with subtree-based filtering.

Xu et al. [58] discuss a subtraction operator and disjointness on types. Their operations are algebraically similar to ours, but serve a type system with records and universal quantification for reasoning about interfaces and overloading rather than capabilities or effects.

**Classifying Specific Capability Classes.** Spores [29] constrain what may appear in a closure’s captured environment, enforcing serialization and concurrency safety. This is close to our **only** and **except** operators, which also restrict which capability values a closure may capture. Spores attach these restrictions to each closure type, whereas our system factors them through a shared, open classifier hierarchy. We further discuss spores and classifier traits in Section 6.5.

Osvald et al. [34] classify values by lifetime scope, and Xhebraj et al. [56] extend this with delayed stack reclamation. Our approach can provide equivalent static guarantees (Section 6.3), though similar stack-allocation optimizations remain future work.

Fractional capabilities and related qualifiers can track ownership and mutability. Haller and Odersky [13] classify references as unique or borrowed. Fractional permissions [6] split read and write access, and Gordon et al. [11] use a mutability lattice. Marshall and Orchard [28] encode fractional ownership with graded modal types. Qualified types [18] likewise attach lattice-based restrictions to values. We do not directly tackle ownership, but classifiers can express closely related distinctions, as discussed in Section 6.3.

**Tracking Exceptions in Types.** While exceptions have been present in programming languages since at least Goodenough [10], many languages omit them from static types. Java’s checked exceptions [12] face exception-polymorphism problems, motivating Scala effect systems [42, 41] and Swift 2’s `throws` clause [1]. Wu et al. [55] model exceptions with scoped effect handlers. Related accounts appear in Eff [3], Koka [19], and Frank [21]. Zhang et al. [65, 64] argue that intercepted exceptions are hard to reason about with higher-order functions and propose “tunneling” exceptions to statically known handlers. Lexical effect handlers in Effekt [7] and Lexa [25] generalize this idea. Odersky et al.’s safer exceptions [32] track exception handlers with capabilities. Lexical handlers still do not match the non-lexical exception semantics of current Scala backends, and Section 6.4 discusses how our classifier-based account builds on safer exceptions.

Delimited continuations can be encoded on top of existing exception mechanisms [17], and tunneling can itself be implemented over Java exceptions [65]. Together with recent Scala continuation work [30, 38], this suggests a route to capture-safe lexical effect handlers across all backends. In Scala, this matters because any practical account has to span the JVM, Native, and JS backends.

**Dynamic Effect Handlers.** Plotkin and Pretnar [39] formalize algebraic effect handlers, Kammar et al. [16] develop their programming idioms, and Yoshioka et al. [63] abstract over the choice of effect representation. A general handler dispatches on the operations of one effect, whereas our `intercept` discharges the open family of labels under one classifier. The route to general handlers in Scala runs through the continuation mechanisms discussed above.

## 8 Conclusion

Capture checking tracks capabilities by identity, but standard library types such as `Try` and `Future` require reasoning about capabilities by *kind*: retaining only control-flow capabilities, or excluding thread-local ones. We introduced capability classifiers, a tree-structured hierarchy of tags with **.only/.except** projections on capture sets, giving precise types to constructs that were previously out of reach. The tree structure ensures disjointness between branches while remaining open to new classifiers in any module. We formalized classifiers as an extension of System Capless, with a decidable kind algebra and kind-annotated projections, and proved type safety via a checked big-step semantics, establishing effect safety, capture prediction, and handler coverage, all mechanized in Lean 4. The system is implemented in the Scala 3 compiler. Overall, classifiers make capture checking more expressive by letting the type system capture the effect distinctions that practical code requires, further strengthening the case for programming with effects and capabilities in a mainstream language.

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## Data Availability Statement

The artifact for this paper [36] includes (1) the Lean 4 mechanization of System Capless( $\mathcal{K}$ ), which proves the safety theorem of Section 4 with its corollaries and the set semantics of the kind algebra (Section 4.1), (2) a snapshot of the Scala 3 compiler with classifiers and the capture-checked standard library (Section 5), (3) the examples of this paper in compilable form, accepted or rejected as claimed, and (4) the case studies compiled by Lutze et al [24], replicated in Scala with classifiers, all accepted by the compiler. Appendix B of the extended report [37] is a guide to the mechanization.

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